# Concentration Quantitatively

DR. MIOY T. HUYNH YALE UNIVERSITY CHEMISTRY 161 FALL 2019

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# **MOLARITY (M): Concentration of solution**

Concentration = 
$$\frac{\text{moles of solute}}{\text{Volume (L) of solution}}$$
;  $M = \frac{\text{mol}}{L}$ 

Think about what concentration means before getting into the math.



Each black dot represents a mole (the quantity/amount)

# What is a ppm?

A ppm (part per million) is a unit of concentration. Specifically, it is:

 $1 \text{ ppm} = \frac{1 \text{ mg solute}}{1 \text{ kg solution}}$ 

A molar (M or mol/L) is a unit of concentration as well. If a solution of NaCl is 0.80 M, we say:  $0.80 \text{ M NaCl} = \frac{0.80 \text{ mol NaCl}}{1 \text{ L}}$ 

Likewise, a solution of NaCl that is 0.80 ppm is:  $0.80 \text{ ppm NaCl} = \frac{0.80 \text{ mg NaCl}}{1 \text{ kg water}}$ 

We can convert between the two units of concentration using the density of water and the molar mass of NaCI:

$$0.80 \text{ ppm NaCl} = \frac{0.80 \text{ mg NaCl}}{1 \text{ kg water}} \times \frac{1 \text{ kg}}{1000 \text{ g}} \times \frac{1 \text{ g water}}{1 \text{ mL water}} \times \frac{1000 \text{ mL}}{1 \text{ L}} \times \frac{1 \text{ g}}{1000 \text{ mg}} \times \frac{1 \text{ mol NaCl}}{58.44 \text{ g NaCl}} = 1.4 \times 10^{-5} \frac{\text{mol}}{\text{L}} \text{ NaCl}$$

Dr. Mioy T. Huynh

Consider separate solutions of NaOH and KCI made by dissolving equal masses of solute in equal volumes of solution. Which solution has the greater concentration?

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NaOH = 39.99 g/mol

KCI = 74.55 g/mol

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$$10 \text{ g NaOH} \times \frac{1 \text{ mol}}{39.99 \text{ g}} = 0.25 \text{ mol NaOH}$$

$$[NaOH] = \frac{\# \text{ moles}}{\text{Volume (L)}}$$
$$= \frac{0.25 \text{ mol NaOH}}{1 \text{ L}}$$
$$= 0.25 \text{ M}$$

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Let's assume you have 10 g of each solute and 1 L of solution.

We can determine the concentration (molarity) of each solution then:

 $10 \text{ g NaOH} \times \frac{1 \text{ mol}}{39.99 \text{ g}} = 0.25 \text{ mol NaOH}$   $10 \text{ g KCl} \times \frac{1 \text{ mol}}{74.55 \text{ g}} = 0.134 \text{ mol KCl}$   $[\text{NaOH}] = \frac{\# \text{ moles}}{\text{Volume (L)}}$   $= \frac{0.25 \text{ mol NaOH}}{1 \text{ L}}$  = 0.25 M  $[\text{KCl}] = \frac{\# \text{ moles}}{\text{Volume (L)}}$   $= \frac{0.134 \text{ mol KCl}}{1 \text{ L}}$ 

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$$[\text{NaOH}] = \frac{\# \text{ moles}}{\text{Volume (L)}}$$

$$= \frac{0.25 \text{ mol NaOH}}{1 \text{ L}}$$

$$= 0.25 \text{ M}$$

$$[\text{KCl}] = \frac{\# \text{ moles}}{\text{Volume (L)}}$$

$$= \frac{0.134 \text{ mol KCl}}{1 \text{ L}}$$

Because NaOH has a smaller molar mass, we have <u>more</u> moles of NaOH  $\rightarrow$  greater concentration/molarity.

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Consider separate solutions of NaOH and KCI made by dissolving 125.0 g of each solute in 250.0 mL of solution. Calculate the concentration of each solution.

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125.0 g NaOH ×  $\frac{1 \text{ mol}}{39.99 \text{ g}}$  = 3.125<sub>8</sub> mol NaOH 125.0 g KCl ×  $\frac{1 \text{ mol}}{74.55 \text{ g}}$  = 1.676<sub>7</sub> mol KCl

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Because NaOH has a smaller molar mass, we have <u>more</u> moles of NaOH  $\rightarrow$  greater concentration/molarity.

Dr. Mioy T. Huynh

We have a 0.800 M solution of NaOH. You need 75.0 mL of a 0.35 M solution. How do you make such a solution?

There are two ways to change the concentration: (1) change the number of moles and (2) change the volume.

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We can find out by setting up the expression for molarity and solving for the # of moles:

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$$[NaOH] = \frac{\# \text{ moles}}{\text{Volume (L)}}$$
$$0.35 \text{ M} = \frac{\text{x mol}}{75.0 \text{ mL} \times \frac{1 \text{ L}}{1000 \text{ mL}}}$$
$$\text{x} = 0.026_3 \text{ mol NaOH}$$

<u>Step 2:</u>

How much of the 0.800 M NaOH solution contains 0.026<sub>3</sub> mol of NaOH?

$$[NaOH] = \frac{\# \text{ moles}}{Volume (L)}$$
$$0.800 \text{ M} = \frac{0.026_3 \text{ mol NaOH}}{V}$$
$$V = 0.032_8 \text{ L}$$

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<u>Step 3:</u>

Find the amount of water needed to dilute this sample:  $\left(75.0 \text{ mL} \times \frac{1 \text{ L}}{1000 \text{ mL}}\right) - 0.032_8 \text{ L} = 0.042 \text{ L} \text{ water}$ 

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You can use the following equation to solve for the volume ( $V_2$ ) of the 0.800 M solution ( $M_2$ ) that would contain the same number of moles as 75 mL ( $V_1$ ) of the 0.35 M solution ( $M_1$ ):

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Find the amount of water needed to dilute this sample:  $\left(75.0 \text{ mL} \times \frac{1 \text{ L}}{1000 \text{ mL}}\right) - 0.032_8 \text{ L} = 0.042 \text{ L water}$ 

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You prepare 525 mL of a 0.50 M HI solution. After three days of sitting on the bench, its molarity if now 0.82 M. How much water has evaporated?

Recognize that we have the same number of moles since only the water evaporates. The concentration increases because we have less volume of water per mole of HI.

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Now find out what volume of the 0.82 M solution contains this many moles of HI:

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Now find out what volume of the 0.82 M solution contains this many moles of HI:  $0.82 \text{ M} = \frac{0.26_3 \text{ mol HI}}{M}$ 

$$V = 0.32 L = 320 mL$$

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Alternative solution:

$$M_1 V_1 = M_2 V_2$$
  
(0.50 M)(525 mL) = (0.82 M)V\_2  
$$V_2 = 320 L$$

Now find out what volume of the 0.82 M solution contains this many moles of HI:  $0.82 \text{ M} = \frac{0.26_3 \text{ mol HI}}{V}$  V = 0.32 L = 320 mL

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## I mix 220 mL of 1.5 M HCI solution with 405 mL of 0.42 M HCI solution. What is the new volume and concentration of this solution?

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$$[HCl]_{1} = \frac{\# \text{ moles}}{\text{Volume (L)}} \qquad [HCl]_{2} = \frac{\# \text{ moles}}{\text{Volume (L)}}$$
$$1.5 \text{ M} = \frac{x_{1} \text{ mol}}{220 \text{ mL} \times \frac{1 \text{ L}}{1000 \text{ mL}}} \qquad 0.42 \text{ M} = \frac{x_{2} \text{ mol}}{405 \text{ mL} \times \frac{1 \text{ L}}{1000 \text{ mL}}}$$
$$x_{1} = 0.33 \text{ mol HCl} \qquad x_{2} = 0.17 \text{ mol HCl}$$

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$$[HCI]_{1} = \frac{\# \text{ moles}}{\text{Volume (L)}} \qquad [HCI]_{2} = \frac{\# \text{ moles}}{\text{Volume (L)}} \qquad n_{HCI} = x_{1} + x_{2} \\ = 0.33 \text{ mol} + 0.17 \text{ mol} \\ n_{HCI} = 0.33 \text{ mol} + 0.17 \text{ mol} \\ n_{HCI} = 0.50 \text{ mol HCl}} \\ n_{HCI} = 0.50 \text{ mol HCl}} \\ x_{1} = 0.33 \text{ mol HCl}} \qquad x_{2} = 0.17 \text{ mol HCl}} \qquad n_{HCI} = 0.50 \text{ mol HCl}}$$

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We can start by finding the number of moles in solution 1, solution 2, and the total:



And the total volume is 220 mL + 405 mL = 625 mL.

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So we can find the new concentration now:

$$[\text{HCl}] = \frac{0.50 \text{ mol HCl}}{62_5 \text{ mL} \times \frac{1 \text{ L}}{1000 \text{ mL}}} = 8.0 \times 10^{-7} \text{ M}$$

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$$[\text{HCl}] = \frac{0.50 \text{ mol HCl}}{62_5 \text{ mL} \times \frac{1 \text{ L}}{1000 \text{ mL}}} = 0.80 \text{ M}$$

Q: Does that make sense?

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Q: Does that make sense?

A: Yes! We diluting our HCl by mixing a greater amount of low concentration HCl into a higher concentration.